



All-particle cosmic ray energy spectrum measured by the HAWC experiment from 10 to 500 TeV

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We report on the measurement of the all-particle cosmic ray energy spectrum with the High Altitude Water Cherenkov (HAWC) Observatory in the energy range 10 to 500 TeV. HAWC is a ground-based air-shower array deployed on the slopes of Volcan Sierra Negra in the state of Puebla, Mexico, and is sensitive to gamma rays and cosmic rays at TeV energies. The data used in this work were taken over 234 days between June 2016 and February 2017. The primary cosmic-ray energy is determined with a maximum likelihood approach using the particle density as a function of distance to the shower core. Introducing quality cuts to isolate events with shower cores landing on the array, the reconstructed energy distribution is unfolded iteratively. The measured all-particle spectrum is consistent with a broken power law with an index of -2.49 ± 0.01 prior to a break at (45.7 ± 0.1) TeV, followed by an index of -2.71 ± 0.01 . The spectrum also represents a single measurement that spans the energy range between direct detection and ground-based experiments. As a verification of the detector response, the energy scale and angular resolution are validated by observation of the cosmic ray Moon shadow's dependence on energy.

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I. INTRODUCTION

The primary cosmic ray spectrum spans a wide range covering over ten decades in energy and thirty decades in flux [1,2]. It is well described by a nearly single power law of index $\gamma \approx -2.7$, with two prominent breaks at $\sim 3 \times 10^{15}$ eV and $\sim 3 \times 10^{18}$ eV, referred to as the “knee” and “ankle,” respectively. The nonthermal nature of the spectrum, including the breaks, carries information regarding the dynamics of the environments in which cosmic rays are accelerated and those that they traverse. Despite significant experimental efforts to study this structure, our understanding of the nature of acceleration sites remains incomplete.

For cosmic ray particles with energy below about 100 TeV, direct measurements from satellite and balloon-borne experiments provide the most detailed measurements of the primary particle spectrum. Recent results from the PAMELA [3] satellite demonstrate a decrease in the proton-to-helium flux ratio up to TV rigidities or \sim TeV energies. Similarly, the CREAM balloon-borne detector [4–6] reports further hardening of the helium energy spectrum, surpassing the proton flux at approximately 10 TeV. The flattening of the helium flux relative to protons also has been reported by the ATIC experiment [7]. This type of structure could be an indication of different source populations [8], or a nearby source that is proton rich up to TeV energies [9]. It has also been suggested that the spectral hardening could be attributed to anomalous diffusion [10].

Probing the cosmic ray spectrum via direct detection becomes a challenge in the 10–100 TeV range and beyond due to limited detector exposures fueled by a rapidly

diminishing flux. Ground-based air-shower arrays are not as limited by their collection area but are not as sensitive to the identity of the primary particle, as well as being reliant on simulations to estimate extensive air-shower parameters. However, as demonstrated by recent results from the ARGO-YBJ [11], GRAPES-3 [12], and Tibet-III [13] experiments, ground-based arrays are best suited to probe the all-particle flux above 100 TeV.

The energy response to hadronic air showers of the High Altitude Water Cherenkov (HAWC) Observatory [14] allows for a detailed measurement of the cosmic ray flux above 10 TeV. This is due in part to the similar size of multi-TeV showers and the containment area of HAWC, as well as the array's proximity to shower maximum at these energies, where shower fluctuations are minimized. This places the HAWC observatory in a position to bridge cosmic ray measurements between direct detection apparatuses and larger PeV-scale air-shower array experiments. In this paper, we demonstrate that ability by reporting on the analysis of the data sample collected by the HAWC experiment in the period from June 2016 to February 2017 and the measurement of the all-particle cosmic ray energy spectrum between 10–500 TeV. The cosmic ray Moon shadow's evolution with energy is presented as a verification of the energy scale in these measurements.

The paper is organized as follows: In Sec. II the main characteristics of the HAWC detector are described. The simulation methods and event sample used for the analysis are described in Sec. III. Section IV is devoted to the data analysis including details of the event selection, event reconstruction, the unfolding method, and sources of systematic uncertainties. The results are presented in Sec. V and discussed in Sec. VI. Section VII summarizes the main conclusions of this work.

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II. THE HAWC OBSERVATORY AND DATA SELECTION

The Earth's atmosphere is opaque to cosmic rays in the energy range of HAWC. Primary cosmic ray particles interact with air molecules to produce large cascades of secondary particles, called extensive air showers. Properties of the primary cosmic ray must be inferred from the air-shower particles that reach ground level. The HAWC Observatory is an air-shower array located at 4100 m above sea level on the slopes of Volcan Sierra Negra in the state of Puebla, Mexico. HAWC is designed to detect air showers produced by primary gamma rays in the 500 GeV to 100 TeV energy range, but its altitude and physical dimensions permit measurements of primary hadronic cosmic rays up to multi-PeV energies.

The detector comprises a 22,000 m² array of 294 close-packed water Cherenkov detectors (WCDs). Each WCD consists of a 4.5 m tall and 7.3 m diameter cylindrical steel tank lined with a black plastic bladder and filled with 188,000 liters of purified water. Attached to the floor of each tank are four upward-facing photo-multiplier tubes (PMTs): one central high-quantum efficiency Hamamatsu 10-inch R7081 PMT, and three 8-inch R5912 PMTs each at 1.8 m from the center forming an equilateral triangle. The PMTs observe the Cherenkov light produced when secondary particles (primarily electrons, positrons, and gamma rays) from air showers enter the tank. Figure 1 depicts the full HAWC array and the schematic of a WCD.

The PMT signals are transferred via RG59 coaxial cables to a central counting house, where they are amplified, shaped, and discriminated on custom front-end boards

using two voltage thresholds: one at 1/4 and the other at 4 photoelectrons (PEs). The time stamps when these thresholds are crossed are recorded and provide a means of inferring the amplitude of the measured signal. The resulting time-over-threshold (ToT) is proportional to the logarithm of the pulse's total charge. Commercial time-to-digital converters (TDCs) digitize the ToTs, and send the data to a farm of computers for further processing. A simple multiplicity trigger is used to identify candidate air-shower events, ensuring that a minimum number of PMTs record signals within a defined time window.

The event reconstruction procedure involves determination of air-shower properties including local arrival direction, core position, and an estimate of the primary energy. While a cursory reconstruction is performed on-site, this analysis uses the results from the fourth revision (Pass-4) of the off-site reconstruction, to have a uniform data set and the most updated calibrations available. The calibration procedure permits the estimation of the true number of PEs in a PMT from the measured ToT. It is performed by an on-site laser system that sends pulses to each WCD while the PMT responses are recorded. A further calibration step is required to account for varying cable lengths resulting in PMT timing differences, which are determined to sub-ns precision.

The HAWC detector in its full configuration was in stable data taking mode during the runs selected for this analysis, amounting to a total live time of 234 days from 8 June, 2016 to 17 February, 2017. The total up-time efficiency was $\sim 92\%$ and the mean trigger rate was ~ 25 kHz. All events triggering at least 75 PMTs and passing the core and angle fitting routines were processed

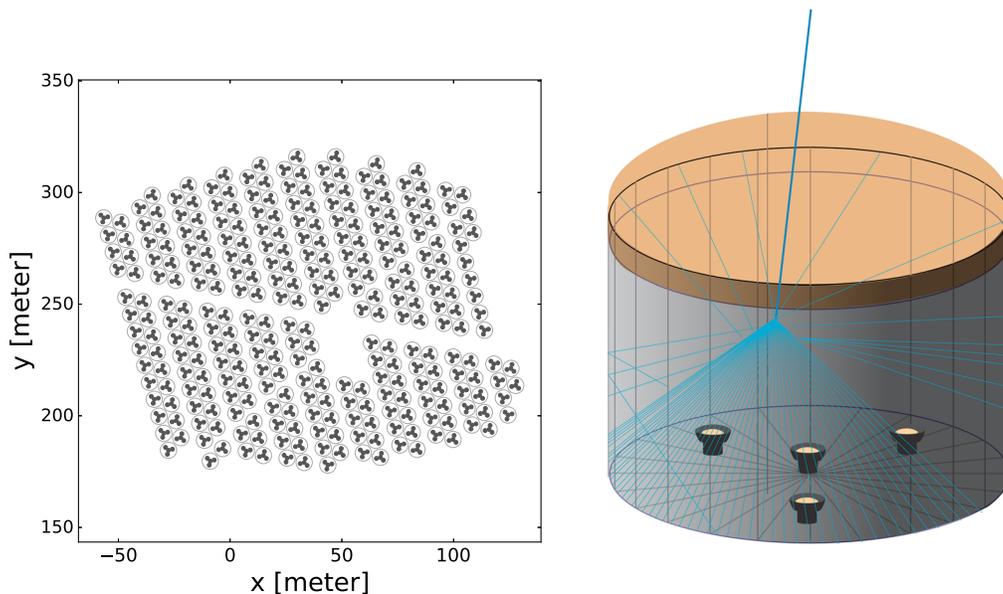


FIG. 1. The left panel shows the layout of the entire HAWC detector. Each WCD is indicated by a large circle encompassing the smaller, darker circles which identify the PMTs. The right panel depicts the representation of a single WCD including the steel tank, the protective roof, and the four PMTs. The penetrating dark blue line represents a high-energy secondary air shower particle, which emits Cherenkov radiation indicated by the cyan rays inside the WCD volume.

for final analysis. Further event selection described in Sec. IV C identifies a data set consisting of 8.42×10^9 events with a mean energy of ~ 3 TeV.

III. SIMULATION

A. Air-shower events

1. Extensive air showers

Extensive air showers are characterized by a laterally extended but thin disk of secondary particles. The nature of the primary particle determines the evolution of the shower with regard to the particle content and subsequently the shape and energy distribution as the shower develops through the atmosphere.

For a primary particle interacting in the atmosphere, the resulting air shower is simulated using the CORSIKA [15] package (v740), with FLUKA [16,17], and QGSJet-II-03 [18] as the low energy and high energy particle physics interaction models, respectively. Smaller simulation sets were generated for hadronic interaction systematic studies using the EPOS (LHC) [19] and SIBYLL 2.1 [20] high energy models.

Primaries of the eight species measured by the CREAM flights [4,6] (H, ^4He , ^{12}C , ^{16}O , ^{20}Ne , ^{24}Mg , ^{28}Si , ^{56}Fe) were generated on an E^{-2} differential energy spectrum from 5 GeV–3 PeV and distributed over a $R_{\text{thrown}} = 1$ km radius circular throwing area. The simulated zenith angle range was 0° – 70° , azimuthally symmetric, and weighted to a $\sin\theta\cos\theta$ arrival distribution. The secondary charged particles interacting with the HAWC detector were simulated using the GEANT4 [21] package. Dedicated HAWC software was used to simulate the detector response over the entire hardware and data analysis chain.

2. Composition

Comparison of the measured Moon shadow with predictions as well as the unfolding of the all-particle spectrum

requires an assumption on the composition of the cosmic-ray spectrum. The spectra of individual primary elements were weighted according to a broken power law of the form

$$\mathcal{F}(A, E_{\text{br}}, \gamma_1, \gamma_2) = \begin{cases} A \cdot \left(\frac{E}{E_0}\right)^{\gamma_1} & E < E_{\text{br}} \\ A \cdot \left(\frac{E_{\text{br}}}{E_0}\right)^{\gamma_1 - \gamma_2} \cdot \left(\frac{E}{E_0}\right)^{\gamma_2} & E \geq E_{\text{br}}, \end{cases} \quad (1)$$

where A is the normalization at E_0 with spectral index γ_1 , and a second index γ_2 starting at energy E_{br} . For all species' fits, $E_0 = 100$ GeV. The nominal composition assumption used in simulation is the best fit of Eq. (1) to direct measurement data provided by AMS [22,23], CREAM [4,6], and PAMELA [3]. The fluxes for proton and helium were allowed to vary independently while those for elements with atomic number $Z > 2$ were varied together and thus have the same spectral indices. The resulting fit values for the various species are presented in Table I, defining the nominal composition model used in this analysis.

B. Moon shadow

The Moon blocks the nearly isotropic flux of cosmic rays on their path to Earth, and because of their charge, cosmic rays interact with the Earth's magnetic field which bends their trajectories. The deflection is dependent on both the particle charge and energy, so this has the effect of shifting the shadow in relation to the Moon's true position. Using an accurate representation of the geomagnetic field, we can compare simulated trajectories to the observed cosmic ray Moon shadow as an independent test of the detector's angular resolution and energy response.

To simulate the cosmic ray Moon shadow, we developed a charged particle propagation routine including geomagnetic effects using the international geomagnetic reference field (IGRF) [24] model. To efficiently generate sufficient statistics to model the shadow, we used the set of 345

TABLE I. Equation (1) parameters for the hadronic species considered for the assumed composition in this analysis. The parameters were obtained as best fits to AMS [22,23], CREAM [4,6], and PAMELA [3] data. Uncertainties in the fits were included in estimating the systematic uncertainties of flux measurements due to composition assumptions.

	A	E_{br}	$-\gamma_1$	$-\gamma_2$
	$[\text{GeV s sr m}^2]^{-1}$	$[\text{GeV}]$		
H	$(4.48 \pm 0.04) \times 10^{-2}$	$440.6^{+87.8}_{-62.7}$	2.81 ± 0.01	2.66 ± 0.01
He	$(3.31 \pm 0.02) \times 10^{-2}$	$854.8^{+125.7}_{-105.5}$	2.73 ± 0.01	2.54 ± 0.01
C	$(6.96 \pm 0.18) \times 10^{-6}$	$2882^{+904.4}_{-481.9}$	2.76 ± 0.03	2.55 ± 0.04
O	$(5.00 \pm 0.09) \times 10^{-6}$	3843^{+1206}_{-643}	2.76 ± 0.03	2.55 ± 0.04
Ne	$(6.31 \pm 0.35) \times 10^{-7}$	4803^{+1507}_{-803}	2.76 ± 0.03	2.55 ± 0.04
Mg	$(5.70 \pm 0.26) \times 10^{-7}$	5764^{+1809}_{-964}	2.76 ± 0.03	2.55 ± 0.04
Si	$(5.70 \pm 0.13) \times 10^{-7}$	6725^{+2110}_{-1124}	2.76 ± 0.03	2.55 ± 0.04
Fe	$(2.00 \pm 0.04) \times 10^{-7}$	13450^{+4220}_{-2249}	2.76 ± 0.03	2.55 ± 0.04

graphics processing units (GPUs) available at the Wisconsin IceCube Particle Astrophysics Center. The OpenCL API specification [25] is used for the GPU kernel invocation, with the host central processing unit (CPU) backend being written with PyOpenCL [26]. Each GPU is capable of simulating the propagation of $\sim 10^6$ particles nearly simultaneously, providing statistics $O(10^9)$ within hour time scales, which translates to a speedup of $90\times$ over available CPU resources.

Particles are backtraced from the location of the HAWC detector until reaching the orbital radius of the Moon and intersection with the Moon sphere is determined. The Boris-Buneman method [27,28] is used to integrate the relativistic equations of motion, due to its symplecticity and wide use in plasma physics applications. Furthermore, we employ a fixed angular displacement step of 10^{-3} rad by sampling the field strength at each numerical integration, serving as an adaptive step in time. This ensures that in regions of higher magnetic field strength where charged particle deflection is greater, the particle trajectory is sampled more finely than where the field strength is weaker. If the maximum allowable number of integration steps (10^4) is reached, the particle is assumed to be below the geomagnetic cutoff and not considered further.

IV. ANALYSIS

To infer shower properties from the raw hit data, events are subject to a reconstruction procedure. The quantities of interest are the shower “direction” and “core location,” which are then used to estimate the primary energy, E_{reco} . A set of selection criteria is applied to improve the quality of the reconstructed event sample and minimize potential bias in our estimate of the detector response. We validate the simulated detector response by the observation of the cosmic ray Moon shadow’s evolution with energy. The all-particle energy spectrum is determined using an iterative unfolding procedure, and sources of systematic uncertainties are taken into account.

A. Direction and core reconstruction

The front of particles in extensive air showers assumes a conical form whose main axis defines the arrival direction and whose apex is the shower core. The highest density of secondary particles coincides with the core location. Farther away, the shower front becomes less dense and wider in time. For the electromagnetic component of an extensive air shower, the expected particle density as a function of the lateral distance from the core is well approximated by the Nishimura-Kamata-Greisen (NKG) function [29]. We implement a modification that includes a Gaussian component, such that the signal amplitude S given a core position \vec{x} at a point \vec{x}_i is given by

$$S(A, \vec{x}, \vec{x}_i) = A \cdot \left(\frac{1}{2\pi\sigma^2} e^{-\frac{|\vec{x}_i - \vec{x}|^2}{2\sigma^2}} + \frac{N}{(0.5 + \frac{|\vec{x}_i - \vec{x}|}{R_m})^3} \right), \quad (2)$$

where A is a normalization factor, R_m is the Molière radius of the atmosphere (approximately 120 m at HAWC altitude), σ is the width of the Gaussian, and N is the normalization of the NKG tail. The values of σ and N are fixed to 10 m and 5×10^{-5} , respectively. The modification ameliorates observed excessive iterations due to the NKG function’s rapidly increasing amplitude near $r = 0$, as well as computationally expensive calls to fitting the exponential involving the age parameter.

The estimated core position \vec{x} and local zenith and azimuth angles (θ , ϕ) are reconstructed in an iterative procedure described in [14]. Using all triggered PMTs in an event, a simple center-of-mass core estimate serves as a seed to the more elaborate lateral distribution function presented in Eq. (2). This core position is then provided to a plane fit estimate of the shower arrival direction. Provided these initial estimates of \vec{x} , θ , ϕ , a selection of PMTs within ± 50 ns of a curvature correction to the shower plane is provided for a final pass of the core and angle fitters. Two example events which have passed the event selection criteria are shown in Fig. 2.

B. Energy estimation

To estimate the primary cosmic ray energy, we use the lateral distribution of the measured signal as a function of the primary particle energy. Using a proton-initiated air-shower simulation, we build a four-dimensional probability table with bins in zenith angle, primary energy, PMT distance from the core in the shower plane (lateral distance), and measured PMT signal amplitude. The table provides the probability for observing a given PMT amplitude Q at a lateral distance R from the shower core in a proton shower of energy E and zenith angle θ . The tables are smoothed with a multidimensional spline fitting routine [30] to ensure bin fluctuations from the simulation statistics do not influence energy estimation. Given a shower with a reconstructed arrival direction and core position, each PMT contributes a likelihood value extracted from the tables, including operational PMTs that do not record a signal. For each possible energy, the logarithms of the likelihood values for all PMTs are summed, and the energy bin with the maximal likelihood value is chosen as the best energy estimate.

The proton energy table takes the following form:

- (1) Three zenith angle bins
 - (a) θ_0 : $0.957 \leq \cos \theta \leq 1$
 - (b) θ_1 : $0.817 \leq \cos \theta < 0.957$
 - (c) θ_2 : $0.5 \leq \cos \theta < 0.817$
- (2) Forty-four energy bins from 70 GeV–1.4 PeV with bin width of 0.1 in $\log E$

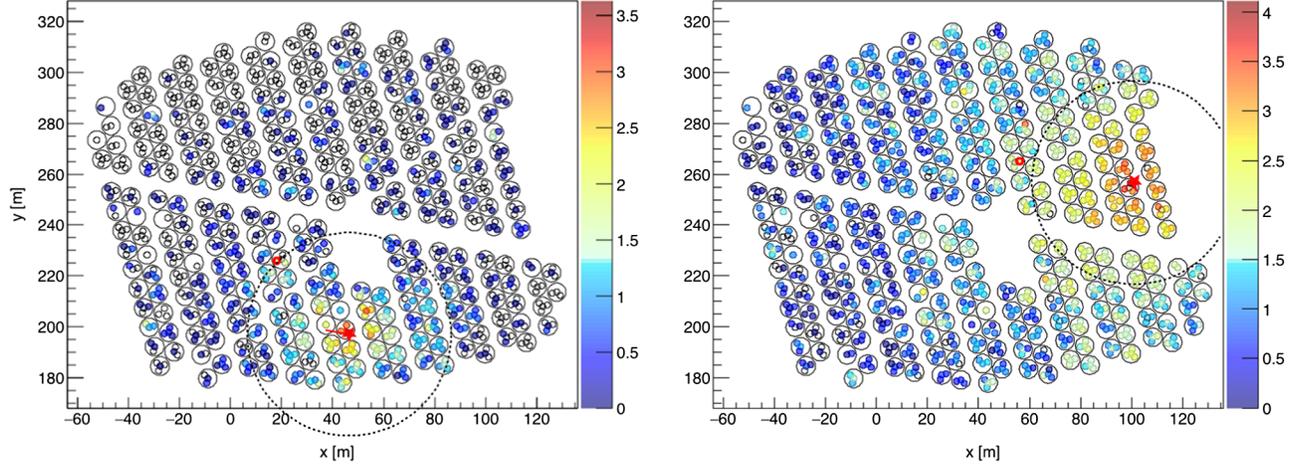


FIG. 2. Example air-shower events from the data sample, where the color scale indicates the logarithm of the measured signal in PEs. The core location is indicated by the red star, and the 40 meter circle shows the region used for N_{r40} . The reconstructed energy of the events are 10 TeV (left) and 100 TeV (right), where the uncertainty on each is 0.1 in $\log E_{\text{reco}}$.

- (3) Seventy bins in lateral distance R from 0–350 m in bins of width 5 m
- (4) Forty bins in charge Q from $1-10^6$ photoelectrons in steps of 0.15 in $\log Q$

The lateral distance bin spacing was assigned half of the spacing between WCD centers, which is of order 10 m. Finally, the charge bin width was chosen to be of the same order as the estimated PMT charge resolution ($\sim 30\%$).

The resulting performance is evaluated via the bias distribution, defined by the difference between the logarithms of the reconstructed and true energy values,

$$\text{bias} = \log E_{\text{reco}} - \log E, \quad (3)$$

shown for a single energy bin in Fig. 3. The mean of this distribution defines the energy bias or offset and the width defines the energy resolution, which are shown as functions of energy in the panels of Fig. 4, provided the event selection criteria. We also identify the integral of the bias distribution as the efficiency $\epsilon(E)$ to reconstruct events at energy E , as the normalization condition includes events that are not reconstructed or do not pass the selection criteria in that energy bin.

Given that the energy estimation tables are built solely from proton simulation, the energy bias for evaluating only proton showers is within half of a table bin width above ~ 4 TeV. This sets an energy threshold below which proton showers just passing the selection cuts will be reconstructed at higher energies, manifesting as an increasingly larger bias with decreasing true energy. This can also be seen as an apparent drop in the energy resolution below ~ 7 TeV due to the decreasing sample size in evaluating Eq. (3).

C. Event selection

The following selection criteria have been adopted for both simulated events and data:

- (a) Events must pass the core and angle fitter, which are required for the energy reconstruction.
- (b) Events must pass a minimum multiplicity threshold of $N_{\text{hit}} \geq 75$ PMTs. This value was chosen in accordance with previous cosmic ray analyses [31], as well as efficiency optimization for the energy reconstruction algorithm which samples the probability tables with $O(10^3)$ PMTs for each energy bin.
- (c) Events are chosen to be within the first zenith angle bin of the energy estimation table. This corresponds to nearly vertical events with $\theta \leq 16.7^\circ$, limiting the

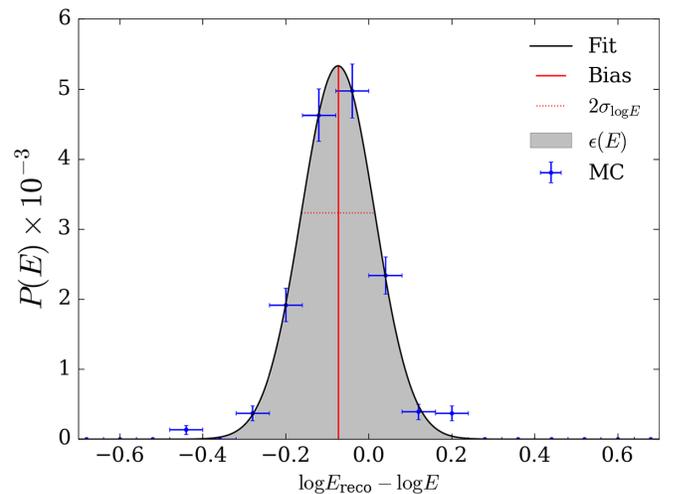


FIG. 3. Difference between the logarithms of the reconstructed E_{reco} and true energy E for the bin centered at $E = 100$ TeV, showing the definitions of energy bias, resolution, and efficiency. The values from simulation are indicated by the blue markers, while the black curve is a Gaussian fit to these points. The normalization condition includes events that were not selected as a result of the selection criteria, thus, the integral represents the efficiency $\epsilon(E)$ to reconstruct and select events in this energy bin.

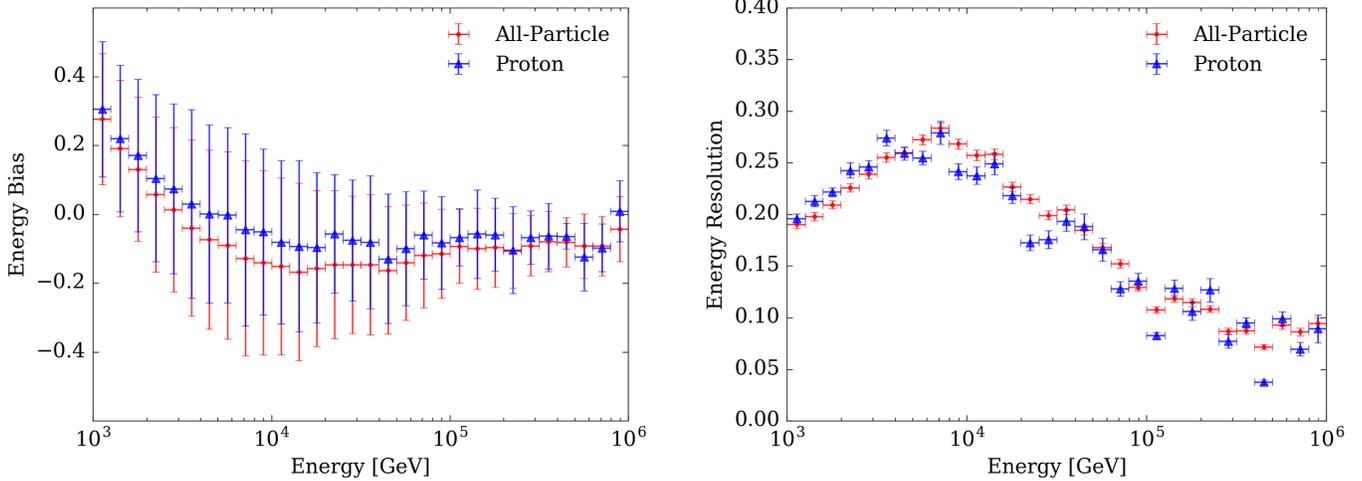


FIG. 4. Resulting energy bias (left) and resolution (right) for all particles and protons as a function of the true energy using the energy estimation method provided the event selection criteria. The vertical bars in the left panel represent the width of the bias distribution or the energy resolution, while the uncertainty in the bias value is comparatively miniscule. The uncertainties shown for the energy resolution are those estimated from the fit of a Gaussian to the bias. The bars in the coordinate represent the bin width in true energy.

influence of shower development from increased atmospheric overburden with increasing zenith angle.

- (d) At least 40 PMTs within 40 meters of the core position ($N_{r40} \geq 40$) must record a signal. This criterion ensures that selected events land on or within 15 meters of the array, resulting in an estimated core resolution of better than 10 meters above 10 TeV. Additionally, the resulting uncertainty in the effective area is below 10%. More harsh values up to $N_{r40} \geq 100$ were tested to further constrain cores to the array with the cost of increasing the uncertainty on the effective area; however, the influence on the measured spectrum was less than 5%. Values less than 20 result in core and angular resolutions above 25 m and 2° , respectively, in addition to causing energy resolutions to exceed 100%.

The effects of making these cuts on simulated and data events are shown in Table II. The core resolution provided by the above selection criteria is estimated to be 10 m at

10 TeV, dropping below 8 m above 100 TeV. The angular resolution above 10 TeV is better than 0.5° .

D. Moon shadow

We applied the event selection criteria and energy estimation technique to the observation of the cosmic ray Moon shadow as a test of the detector response. The zenith angle cut was relaxed to $\theta \leq 45^\circ$ in order to obtain sufficient statistics for a significant observation of the shadow. The resulting sample size is 4.2×10^{10} events. We follow the methods presented in [31,32] for making sky maps. Eleven Moon-centered maps were made in reconstructed energy bins of width 0.2 in $\log E_{\text{reco}}$ from 1–100 TeV, and the true energy of each bin was estimated from simulation. The observed deficit of the Moon shadow is measured with relative intensity, giving the amplitude of deviations from the isotropic expectation,

$$\delta I(\alpha_i, \delta_i) = \frac{N_i - \langle N \rangle_i}{\langle N \rangle_i}, \quad (4)$$

TABLE II. Passing percentages for successive application of event quality cuts in simulation and data, including the observed event rate in data. The percentages represent the fraction of events that passed the previous cut, with the set of triggered events being the reference selection.

Cut	% Passing		Data Event Rate
	MC	Data	[kHz]
No cut (trigger threshold)	100%	100%	24.7
Core & angle fit pass	99%	96%	23.6
$N_{\text{hit}} \geq 75$	31%	23%	5.7
$\theta < 17^\circ$	8%	6%	1.5
$N_{r40} \geq 40$	2%	2%	0.43

where $\langle N \rangle_i$ is the estimated background counts and N_i the observed counts in bin i with right ascension and declination α_i and δ_i , respectively. An example of the Moon shadow observed at an estimated energy of 4.3 TeV is shown in Fig. 5. For each map, the resulting Moon shadow was fit to a two-dimensional Gaussian, from which the offset to the true Moon position in declination ($\Delta\delta$) and right ascension ($\Delta\alpha$) were evaluated. The resulting dependency of the combined angular offset was compared to the expected deviation from simulation, taking into account the detector response and the composition assumption defined in Sec. III A 2.

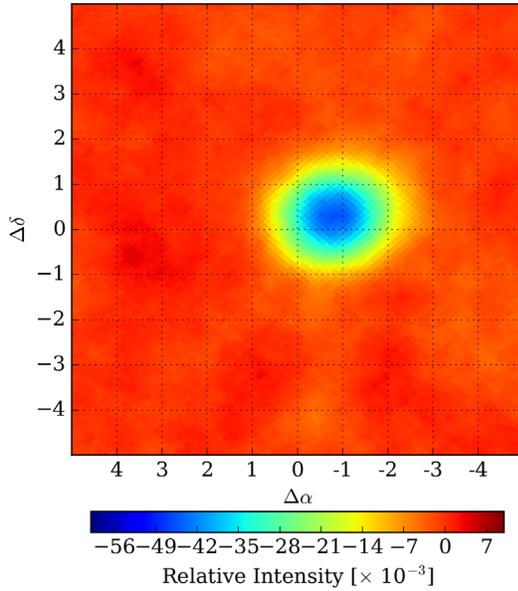


FIG. 5. Relative intensity of the Moon shadow at a mean energy of 4.3 TeV. The map has been smoothed with a top-hat function by 1° to enhance the shadow visually. A two-dimensional Gaussian was fit to the unsmoothed maps.

From the simulation described in Sec. III B, we determined the geomagnetic deflection angle $\delta\omega$ of particles with energy E and charge Z arriving at HAWC to be approximately summarized by

$$\delta\omega \approx 1.59^\circ \cdot Z \left(\frac{E}{\text{TeV}} \right)^{-1}, \quad (5)$$

being inversely proportional to the particle rigidity and consistent with previous studies [33]. We expect the deflection primarily to be in right ascension, with a small $O(0.15^\circ Z/E)$ deviation in declination. Since the cosmic ray spectrum is a mixture of species and the maps are binned in energy, we use the composition model from Sec. III A 2 to estimate the expected mean charge from simulation: $\bar{Z}_{\text{MC}} = 1.23 \pm 0.02$. From the deviation of the observed Moon shadow, we find a mean value of $\bar{Z} = 1.25 \pm 0.06$. The evolution of the offset with energy is depicted in the top panel of Fig. 6, along with the best fit to Eq. (5) and the expectation from simulation. The measured width of the shadow also serves as an experimental verification of the angular resolution, having accounted for the angular width of the Moon disc ($\sim 0.52^\circ$) [31,32]. The fraction of events contained within the 1σ region of the two-dimensional Gaussian fit to the Moon shadow is 46.6%, so we identify the simulated angular deviation value having the same containment fraction. The comparison of the angular resolution estimated from data and simulation is shown in the bottom panel of Fig. 6, and we find that $\chi_{\text{red}}^2 = 11.33/10$.

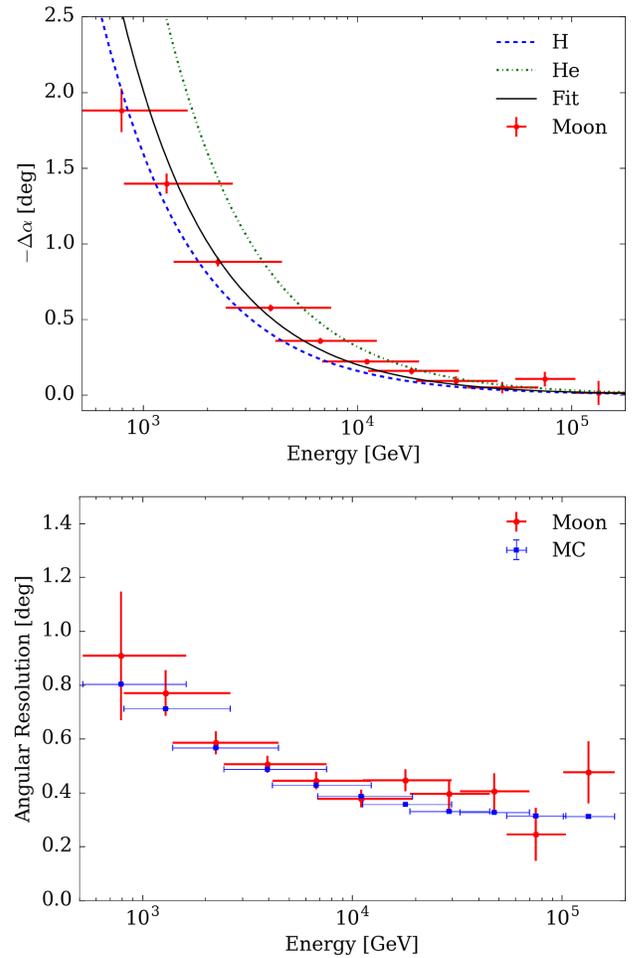


FIG. 6. Top panel: Gaussian centroid offset in right ascension $\Delta\alpha$, with expectations for pure proton and pure helium hypotheses. Fitting the data values to Eq. (5) shown by the black curve results in an estimated mean charge of $\bar{Z} = 1.25 \pm 0.06$. Bottom panel: angular resolution from simulation compared to that estimated from using the Moon shadow width. The Moon points represent the fit widths and are compared to the 46.6% containment fraction from the simulated angular deviation distribution. The uncertainties on the red data points are obtained from the fit to the two-dimensional Gaussian, while the coordinate bins represent the estimated mean and covariance in true energy of each map.

E. Unfolding of the energy spectrum

Extensive air-shower development is subject to inherently large fluctuations, which result in the smearing of the primary particle's estimated energy. Including detector effects such as limited core and angular resolutions must also be taken into account in order to measure the cosmic ray flux. Following the iterative method presented in [34], the observed reconstructed energy distribution is unfolded with the estimated energy response to obtain the measured all-particle energy distribution.

The number of events observed in time T , within the solid angle Ω , and with reconstructed energy E_{reco} ,

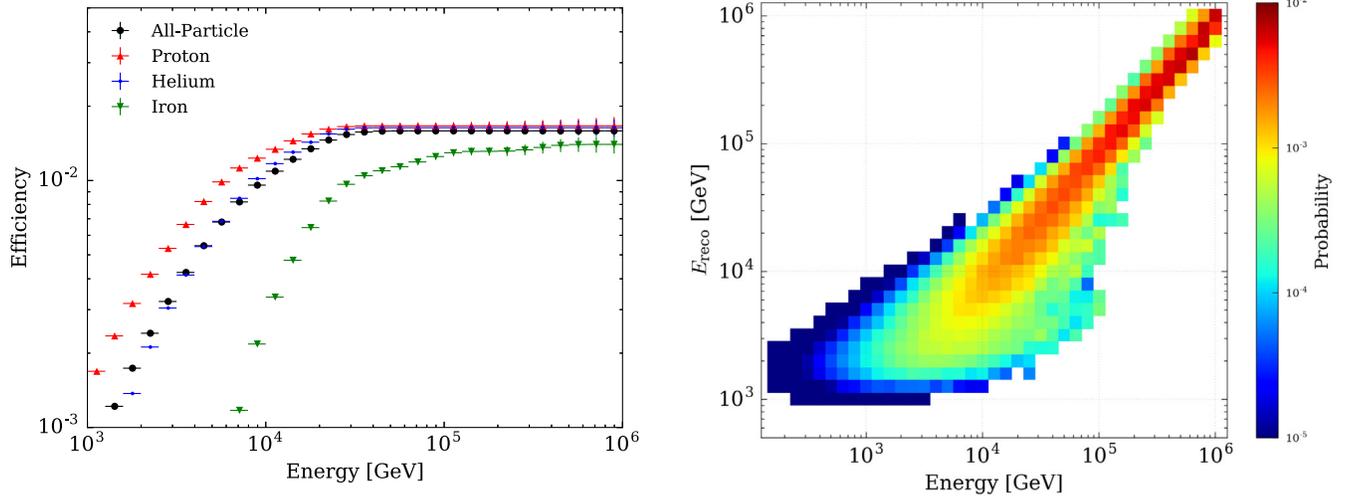


FIG. 7. The left panel shows the efficiencies $\epsilon(E)$ for all combined cosmic ray particles and individually for proton, helium, and iron components. The energy response matrix $P(E_{\text{reco}}|E)$ for all species using the composition defined in Table I is shown on the right. The deviation from the diagonal and the width of $P(E_{\text{reco}}|E)$ are simply the bias and resolution, respectively, already presented in Fig. 4.

$N(E_{\text{reco}})$, is related to the true energy distribution $N(E)$ by the detector effective area $A_{\text{eff}}(E, E_{\text{reco}})$ via

$$N(E_{\text{reco}}) = \frac{1}{\Omega} \int A_{\text{eff}}(E, E_{\text{reco}}) N(E) dE, \quad (6)$$

where $\Omega = 2\pi(\cos\theta_{\min} - \cos\theta_{\max})$, and we have assumed that the detector acceptance depends only weakly on θ due to our restricting events to be nearly vertical. The integration is performed over the range spanned by the true energy limits of A_{eff} .

The effective area is constructed using simulation, and can be summarized by

$$A_{\text{eff}}(E, E_{\text{reco}}) = A_{\text{thrown}} P(E_{\text{reco}}|E), \quad (7)$$

with the simulated throwing area $A_{\text{thrown}} = \pi/2(\cos\theta_{\max} + \cos\theta_{\min})R_{\text{thrown}}^2$, which includes a geometric factor from the zenith angle limits defined by θ_0 as per Sec. IV C; the throwing radius $R_{\text{thrown}} = 1$ km; and $P(E_{\text{reco}}|E)$, the probability for an event with energy E to pass the event selection criteria and reconstructed with energy E_{reco} .

The effective area for a shower of energy E is found by integrating Eq. (7) over E_{reco} ,

$$A_{\text{eff}}(E) = A_{\text{thrown}} \epsilon(E), \quad (8)$$

where $\epsilon(E)$ is the efficiency to observe an event with energy E ,

$$\epsilon(E) = \int P(E_{\text{reco}}|E) dE_{\text{reco}}, \quad (9)$$

and the integration limits cover the reconstructed energy range spanned by the effective area. The object $P(E_{\text{reco}}|E)$

is binned in both E_{reco} and E , forming the energy response matrix and converting the integrals in Eqs. (6) and (9) to summations. The efficiency and response matrix for all species given the event selection criteria are shown in Fig. 7. The nominal composition model from Table I is also taken into account, as species' abundances must be assumed in order to build the all-particle efficiency and response matrix, with effects of other composition models included as systematic uncertainty of the final spectrum.

Provided a prior assumption of the energy distribution with $P(E)$, we construct the unfolding matrix via

$$P(E|E_{\text{reco}}) = \frac{P(E_{\text{reco}}|E)P(E)}{\epsilon(E)\sum_{E'} P(E_{\text{reco}}|E')P(E')}, \quad (10)$$

which defines the probability of a shower with reconstructed energy E_{reco} to have been produced by a primary particle with energy E . The unfolded energy distribution is given by convolving the unfolding matrix with the reconstructed energy distribution via

$$N(E) = \sum_{E_{\text{reco}}} N(E_{\text{reco}}) P(E|E_{\text{reco}}). \quad (11)$$

The analysis is performed iteratively: starting with an initial prior, the $P(E|E_{\text{reco}})$ are computed via Eq. (10), providing a posterior distribution from Eq. (11). This updated distribution is used as the subsequent prior estimate, a procedure that ends once variations on $N(E)$ from one iteration to the next are negligible. For this analysis, a Kolmogorov-Smirnov test [35,36] defined the convergence criterion, where if the test statistic comparing the unfolded distributions between iterations resulted in a p -value less than 0.001, the unfolding was said to have converged. The propagation of uncertainties on $N(E)$ due

to the finite number of simulated and observed air-shower events used in the unfolding procedure follows the analytic prescription derived in Appendix B of [37]. The differential flux is calculated from the final $N(E)$ according to the following relation:

$$\mathcal{F}(E) = \frac{N(E)}{T\Omega A_{\text{eff}}\Delta E}, \quad (12)$$

where T is the observation time, Ω is the solid angle, and ΔE is the energy bin width centered at E .

V. RESULTS

A. The unfolded spectrum

The distribution of reconstructed energy $N(E_{\text{reco}})$ provided the event selection criteria is shown in Fig. 8. Apart from the rise to the peak at $E_{\text{reco}} = 2$ TeV where the detector efficiency is changing rapidly, there is evidence that a change in the spectral index is present between 10–50 TeV in E_{reco} . The unfolded differential spectrum is shown in Fig. 9, including only the systematic uncertainties from the limited simulation sample used to construct the detector response function. Due to the large data set involved, the statistical errors are not visible. The unfolding converged in four iterations, where a noninformative prior was chosen as the starting distribution, and regularization via a spline fit was applied at each iteration. Other priors of power-law form were tested with negligible effect on the final spectrum, and similar results were found when unfolding without regularization and with power-law regularization.

The scaled differential flux reveals a feature which is not well described by a single power law within statistical and simulation uncertainties. The apparent feature below

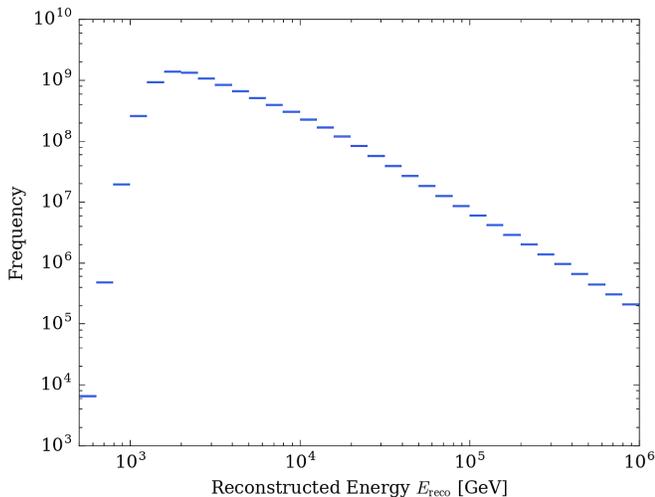


FIG. 8. Reconstructed energy distribution $N(E_{\text{reco}})$ of the data sample used in this analysis. A subtle change in slope above $E_{\text{reco}} = 2$ TeV suggests a change in spectral index between 10–50 TeV in E_{reco} .

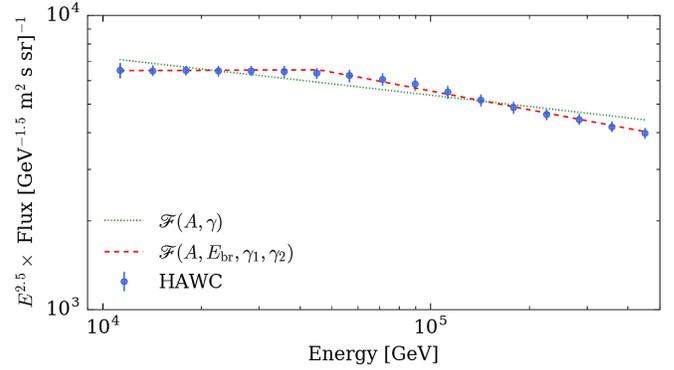


FIG. 9. Unfolded all-particle differential energy spectrum scaled by $E^{2.5}$. The uncertainties visible on the data are the systematic uncertainties from the finite size of the simulated data set, while the statistical uncertainties are smaller than the marker size. Fits to the flux using single $\mathcal{F}(A, \gamma)$ and broken $\mathcal{F}(A, E_{\text{br}}, \gamma_1, \gamma_2)$ power-law forms are also shown by the dashed lines. The broken power law is favored, as for $\Delta\chi^2 = 29.2$ with a difference of two degrees of freedom gives a p -value of 4.6×10^{-7} .

50 TeV in true energy implies a change in the spectral index, so it was fit to a broken power law of the form of Eq. (1) and to a single power law for comparison, both shown in Fig. 9. The best fit single power law has a spectral index of $\gamma = -2.63 \pm 0.01$, while the broken power-law fit resulted in $\gamma_1 = -2.49 \pm 0.01$ and $\gamma_2 = -2.71 \pm 0.01$. The difference in goodness of fit is $\Delta\chi^2 = 29.2$, which for a difference of two degrees of freedom between the two models results in a p -value of 4.6×10^{-7} . Thus, the broken power law is the favored model, and the fit suggests a change in spectral index of about -0.2 at a break energy of $E_{\text{br}} = (45.7 \pm 1.1)$ TeV.

Since the N_{r40} variable’s main effect is to select reconstructed cores, and by extension true cores, within the array, increasing the cut severity should improve the core resolution, and thus the event quality and constraints on the spectral shape. If, for example, the underestimated energies from poor core fits induced a feature in the spectrum, then the fit E_{br} should shift with different cuts. However, we find that the fit normalizations and spectral indices for all harsher criteria agree to within 3%, and the location of the break energy from the fit varies by less than half the bin width ($\Delta \log E = 0.1$). Thus, we find that the spectral feature is insensitive to stronger event selection. We also tested the response to simulated spectra and found that single power-law spectra do not induce features, whereas spectral breaks are recovered from the injection of broken power laws.

B. Systematics

A thorough study of the possible systematic effects has been performed. The main sources of systematic uncertainty considered in this work are

TABLE III. Summary of systematic uncertainties. The contribution from each source was determined by varying that source independently, while holding all others fixed at their nominal values. The contributions from all sources are added in quadrature to conservatively estimate the total systematic uncertainty.

	10 TeV	100 TeV	1 PeV
PMT QE	$\pm 6\%$	$\pm 8\%$	$\pm 9\%$
PMT Q_{res}	-3%	-5%	-10%
Simulation	$\pm 8\%$	$\pm 8\%$	$\pm 8\%$
Composition	$-16/ + 5\%$	$-4/ + 3\%$	$\pm 3\%$
Hadronic Int.	$+5\%$	$+10\%$	$-4/ + 2\%$
Total	$-20/ + 12\%$	$-14/ + 15\%$	$-20/ + 13\%$

- (1) Effects due to the uncertainty in PMT performance properties. This includes the PMT charge resolution, Q_{res} , and the quantum efficiency, QE.
- (2) Effects from the limited statistics from simulation used to build the $P(E_{\text{reco}}|E)$.
- (3) Effects related to the assumed composition model used to build the response function.
- (4) Effects from the hadronic interaction models used in the air-shower simulations.

Table III summarizes the various contributions to the overall systematic uncertainty in three energy bins. We quantified these uncertainties by building a response matrix for each of the various effects. The observed data distribution $N(E_{\text{reco}})$ was then unfolded using each model, and the resulting spectra were compared to the flux unfolded using the nominal response matrix to obtain the fractional deviation of the flux. We do not consider uncertainty in the

energy scale as a source of systematic uncertainty, though for reference we show in subsequent figures the shift in flux that would result from varying the energy values by $\pm 10\%$.

The measurements of the all-particle energy spectrum including both systematic and statistical uncertainties are given in Table IV. The total systematic uncertainty is obtained by adding the contributions from all sources in quadrature. This is a conservative estimate following the work presented in [14], and further study of the interplay of systematic effects is ongoing. The statistical uncertainties are negligible ($\ll 1\%$) due to the large (8×10^9) event sample.

1. PMT charge resolution and quantum efficiency

For a fixed illumination, PMT charge measurements can vary. We summarize this by the charge resolution, Q_{res} , estimated to be between 10–25%. The PMTs also have an intrinsic efficiency (QE) for the combined conversion of an incident photon to a PE and collection of that PE, with typical values between 20–30% [33]. As a result, we vary QE and Q_{res} values in simulation to obtain combined uncertainties on the energy spectra that are approximately 5% below 100 TeV and no larger than 10% at the highest energies.

2. Detector simulation

The energy resolution between 10–500 TeV given the event selection is approximately 25–50%. This is not considered as a systematic error, as it is taken into account in the unfolding procedure. However, the limited statistics

TABLE IV. Values of the all-particle cosmic-ray energy spectrum from 10–500 TeV including uncertainties. The second column is the number of events unfolded, or the distribution $N(E)$. The label “stat” represents the statistical uncertainties, “sys_{MC}” is for the uncertainties from the limited amount of simulation, and “sys” represents the remaining sources of systematic uncertainty added in quadrature.

$\log E/\text{GeV}$	N_{events} Unfolded	$\frac{dN}{dE d\Omega dt dA} \pm \text{stat} \pm \text{sys}_{\text{MC}} + \text{sys} - \text{sys} [\text{GeV s m}^2 \text{sr}]^{-1}$
4.0–4.1	2.00×10^{10}	$(4.7968 \pm 0.0002 \pm 0.5901 + 0.4288 - 0.8530) \times 10^{-7}$
4.1–4.2	1.42×10^{10}	$(2.6922 \pm 0.0001 \pm 0.2323 + 0.2360 - 0.4467) \times 10^{-7}$
4.2–4.3	1.00×10^{10}	$(1.5163 \pm 0.0001 \pm 0.1189 + 0.1315 - 0.2356) \times 10^{-7}$
4.3–4.4	7.08×10^9	$(8.4947 \pm 0.0007 \pm 0.7137 + 0.7352 - 1.2419) \times 10^{-8}$
4.4–4.5	5.02×10^9	$(4.7823 \pm 0.0005 \pm 0.3896 + 0.4171 - 0.6614) \times 10^{-8}$
4.5–4.6	3.54×10^9	$(2.6761 \pm 0.0003 \pm 0.2536 + 0.2377 - 0.3522) \times 10^{-8}$
4.6–4.7	2.47×10^9	$(1.4823 \pm 0.0002 \pm 0.1305 + 0.1357 - 0.1869) \times 10^{-8}$
4.7–4.8	1.71×10^9	$(8.1839 \pm 0.0015 \pm 0.8041 + 0.7830 - 0.9947) \times 10^{-9}$
4.8–4.9	1.18×10^9	$(4.4769 \pm 0.0010 \pm 0.4488 + 0.4547 - 0.5281) \times 10^{-9}$
4.9–5.0	8.03×10^8	$(2.4193 \pm 0.0007 \pm 0.2504 + 0.2655 - 0.2787) \times 10^{-9}$
5.0–5.1	5.34×10^8	$(1.2781 \pm 0.0004 \pm 0.1349 + 0.1544 - 0.1447) \times 10^{-9}$
5.1–5.2	3.56×10^8	$(6.7636 \pm 0.0027 \pm 0.6441 + 0.9164 - 0.7576) \times 10^{-10}$
5.2–5.3	2.37×10^8	$(3.5835 \pm 0.0017 \pm 0.3331 + 0.5544 - 0.3995) \times 10^{-10}$
5.3–5.4	1.59×10^8	$(1.9107 \pm 0.0011 \pm 0.1644 + 0.3430 - 0.2134) \times 10^{-10}$
5.4–5.5	1.09×10^8	$(1.0346 \pm 0.0007 \pm 0.0892 + 0.2184 - 0.1166) \times 10^{-10}$
5.5–5.6	7.25×10^7	$(5.4882 \pm 0.0047 \pm 0.4659 + 1.3920 - 0.6286) \times 10^{-11}$
5.6–5.7	4.87×10^7	$(2.9284 \pm 0.0030 \pm 0.2402 + 0.9642 - 0.3441) \times 10^{-11}$

from simulation used in determining the $P(E_{\text{reco}}|E)$ were taken into account as a source of uncertainty, amounting to less than 8% for the all-particle spectrum.

3. Composition model

We considered two contributions to the uncertainty from the assumed composition models. The first arises from the fit uncertainties of Eq. (1) in defining the nominal CREAM model. We quantified this by varying the fit parameters to within their estimated uncertainties, obtaining the model's contribution to the uncertainty in the unfolded flux. This amounted to less than 3% uncertainty for all energies. We also considered three other widely used models: H4a [38], Polygonato [39], and the Gaisser-Stanev-Tilav model (GST4-gen) [40]. The H3a model also presented in [38] was considered; however, the unfolded spectrum was within <1% of the unfolded spectrum using the H4a model, so we simply quote the H4a result. We take the full range spanned by the models in each energy bin as a conservative estimate of the systematic uncertainty, as we have assumed no preference for any one model.

In all, the uncertainty due to the assumed composition does not exceed +5% for all energies and is within -4% above 100 TeV. The greatest deviation from the nominal model comes from H4a, providing an uncertainty of -16% at 10 TeV. This is due to the significantly larger contribution of heavy elements (>He) to the model as compared to the other three. This has the effect of reducing the efficiency (or equivalently A_{eff}), which can be seen in Fig. 7, since the all-particle efficiency is an abundance-weighted average for all species. The greater presence of heavier elements also induces increased energy migration such that reconstructed events at lower energies are promoted towards higher energies in the unfolded flux.

4. Hadronic interaction model

We also considered the systematic uncertainty from different hadronic interaction models by comparing the nominal simulation using QGSJet-II-03 [18] to the EPOS (LHC) [19] and SIBYLL 2.1 [20] high energy models. The unfolded spectra using the EPOS model and the nominal simulation agree to within 2%, while the spectrum unfolded using the SIBYLL model is systematically higher by between 5–10% for all energies. Studies from groups such as the GRAPES-3 air-shower experiment [12] found that for a fixed composition assumption, the choice of hadronic interaction model influenced the relative abundance of the species arriving at ground level. They found this was primarily due to model differences in determining the point of the first interaction. As the simulated data sets for these models were smaller than the nominal set, a more thorough analysis of the origin of these discrepancies was not possible. Still, we include this as a source of systematic uncertainty using the observed ranges of unfolded spectra.

VI. DISCUSSION

A comparison of the unfolded all-particle spectrum to other recent (<20 yrs) experimental results is shown in Fig. 10. Above 100 TeV, there is agreement with the final ATIC-2 [7] data point though it has statistical uncertainty greater than the HAWC systematics. The HAWC measurement is systematically higher than measurements from other ground-based experiments such as the GRAPES-3 [12] and Tibet-III [13] arrays, but consistent within the estimated systematic uncertainties. Indeed, these discrepancies can be understood as arising from differences in the experiments' energy-scale calibrations. For example, a 10% systematic shift in energy results in a more dramatic ~30% shift in the energy-scaled flux. The ARGO-YBJ spectrum [11] is also lower and appears harder with an index of -2.62 ± 0.03 until ~700 TeV where it softens, so the energy-scaling effect does not address this discrepancy in spectral shape. For comparison, the spectral index as measured by Tibet-III between 150–1000 TeV is -2.68 ± 0.02 , where the uncertainties quoted are statistical and whose value is consistent with that of γ_2 .

In the 10 TeV range, the HAWC spectrum is consistent with the ATIC-2 all-particle measurement [7], including its rise to 30 TeV. The slightly steeper spectrum below 50 TeV is also mirrored, though not as strongly, in the GST4-gen

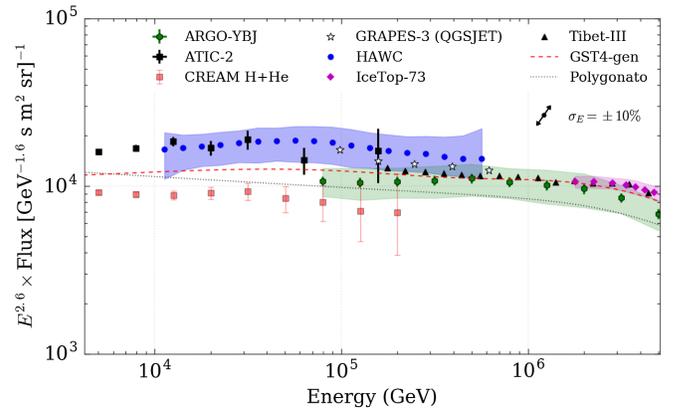


FIG. 10. The differential all-particle energy spectrum measured by HAWC (blue) compared with the spectra from the ARGO-YBJ [11], ATIC-2 [7], GRAPES-3 [12], IceTop [41], and Tibet-III [13] experiments. The CREAM [6] light component spectrum (H + He) is also included for comparison. The uncertainties on the ATIC-2 and CREAM measurements represent combined statistical and systematic uncertainties. For the HAWC, ARGO-YBJ, and IceTop spectra, the shaded regions represent the reported systematic uncertainties. Only ARGO-YBJ reports statistical uncertainties that are shown by visible vertical bars, while for the remaining air-shower array measurements, these are smaller than the respective marker size. The double-sided arrow indicates the shift in flux that would result from a $\pm 10\%$ shift in the energy scale. The GST4-gen [40] and Polygonato [39] all-particle flux models are shown by the red and black dashed lines, respectively.

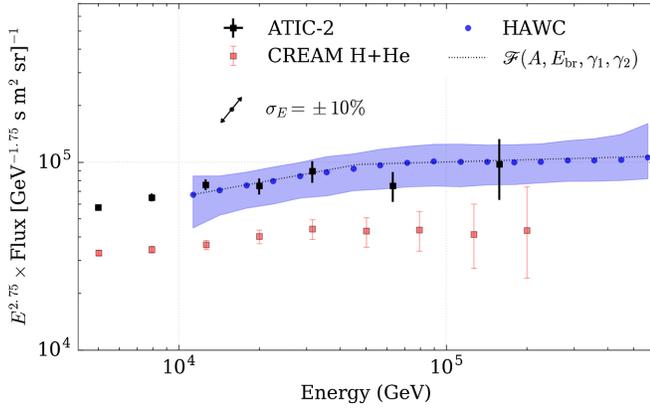


FIG. 11. Comparison of the HAWC spectrum to the all-particle measurement by ATIC-2 [7] and the light component (proton and helium) by CREAM [6]. The energy flux is scaled by $E^{2.75}$ for ease of viewing, and the dashed line is the best fit broken power law $\mathcal{F}(A, E_{\text{br}}, \gamma_1, \gamma_2)$ to HAWC data from Fig. 9 to highlight the location of E_{br} . The double-sided arrow indicates the shift in flux that would result from a $\pm 10\%$ shift in the energy scale.

model, which also depicts a downturn in the 50–60 TeV region. The ARGO-YBJ light-component (proton and helium) measurement [42] does not indicate a spectral softening at these energies, having a constant slope of -2.61 ± 0.04 from 5–280 TeV. There is evidence reported by CREAM [6] of a softening of the helium spectrum between 10–30 TeV, with both proton and helium subsequently becoming softer, though CREAM only reports a single power-law index for each species: -2.66 ± 0.02 and -2.58 ± 0.02 , respectively. For the nominal composition model used in this work, the broken power-law fits from Table I do not indicate spectral softening near 20–40 TeV; however, these fits were merely used to extrapolate composition data into the >10 TeV regime. The ATIC-2 combined proton and helium measurement also shows evidence of a spectral softening, though it peaks near 12 TeV [7]. Figure 11 shows a closer view of this region, comparing the ATIC-2, CREAM, and HAWC spectra. The stronger energy scaling ($E^{2.75}$) of the ordinate reveals consistent spectral forms, with a potential kink between 20–40 TeV for ATIC-2 and a clearer break at 30 TeV for CREAM. Since the light component comprises $\sim 90\%$ of the all-particle flux, these direct detection experiments suggest that proton and helium are responsible for the structure observed in the HAWC measurement.

VII. CONCLUSIONS

The special features of the HAWC experiment—full coverage, high altitude location—allow the imaging of the front of showers induced by primaries with energies down to a few TeV, so far accessible only with balloon-borne experiments, and nearly up to PeV energies. By requiring

near vertical showers and applying a selection criterion based on the particle density near the fit core, a sample of events mainly induced by hadronic showers landing on the array has been selected. Using a technique that relies on evaluating the signal as a function of lateral distance from the fit core, a proton hypothesis-based likelihood table provides the energy estimate for air-shower events. The estimator was verified using the evolution of the cosmic ray Moon shadow, in agreement with the expected deviation with energy from a novel GPU-based simulation. We built a function that connects the true energy to the estimated energy for all cosmic ray species, assuming a CREAM-like composition model. Using this detector response, an iterative unfolding technique has been applied to obtain the differential all-particle cosmic ray energy spectrum in the energy range 10–500 TeV with estimated systematic uncertainties not exceeding 20%.

The HAWC all-particle cosmic ray spectrum exhibits agreement within estimated systematic uncertainties with various experiments from 10–500 TeV, including evidence of a spectral break below 50 TeV. The measurement demonstrates that HAWC can extend the reach of ground-based air-shower arrays into the energy range covered by direct detection experiments. Furthermore, it is with a single experimental technique that the HAWC spectrum bridges these regions. It is also evident that HAWC has the potential to extend the spectrum up to PeV energies to probe the knee. However, as the current event quality selection limits the range to around 500 TeV, an improved understanding of the detector response to the highest energy events is needed.

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- [1] J. Hörandel, The origin of galactic cosmic rays, *Nucl. Instrum. Methods Phys. Res., Sect. A* **588**, 181 (2008).
- [2] J. Blümer, R. Engel, and J. Hörandel, Cosmic rays from the knee to the highest energies, *Prog. Part. Nucl. Phys.* **63**, 293 (2009).
- [3] O. Adriani *et al.* (PAMELA Collaboration), PAMELA measurements of cosmic-ray proton and helium spectra, *Science* **332**, 69 (2011).
- [4] H. Ahn *et al.*, Energy spectra of cosmic-ray nuclei at high energies, *Astrophys. J.* **707**, 593 (2009).
- [5] H. S. Ahn *et al.*, Discrepant hardening observed in cosmic-ray elemental spectra, *Astrophys. J. Lett.* **714**, L89 (2010).
- [6] T. Yoon *et al.*, Cosmic-ray proton and helium spectra from the first CREAM flight, *Astrophys. J.* **728**, 122 (2011).
- [7] A. D. Panov *et al.*, Energy spectra of abundant nuclei of primary cosmic rays from the data of ATIC-2 experiment: final results, *Bull. Russ. Acad. Sci.: Phys.* **73**, 564 (2009).
- [8] V. I. Zatsepin and N. V. Sokolskaya, Three component model of cosmic ray spectra from 10 GeV to 100 PeV, *Astron. Astrophys.* **458**, 1 (2006).
- [9] N. Tomassetti, Origin of the proton-to-helium ratio anomaly in cosmic rays, *Astrophys. J. Lett.* **815**, L1 (2015).
- [10] A. Lagutin and A. Tyumentsev, Proton to helium ratio in cosmic rays: analysis of the PAMELA data, *J. Phys. Conf. Ser.* **409**, 012043 (2013).
- [11] G. Di Sciascio *et al.* (ARGO-YBJ Collaboration), Measurement of the Cosmic Ray Energy Spectrum with ARGO-YBJ, [arXiv:1408.6739](https://arxiv.org/abs/1408.6739).
- [12] H. Tanaka *et al.*, Studies of the energy spectrum and composition of the primary cosmic rays at 100-1000 TeV from the GRAPES-3 experiment, *J. Phys. G* **39**, 025201 (2012).
- [13] M. Amenomori *et al.*, The energy spectrum of all-particle cosmic rays around the knee region observed with the Tibet-III air-shower array, *Adv. Space Res.* **42**, 467 (2008).
- [14] A. U. Abeysekara *et al.*, Observation of the Crab Nebula with the HAWC gamma-ray observatory, *Astrophys. J.* **843**, 39 (2017).
- [15] D. Heck, G. Schatz, T. Thouw, J. Knapp, and J. Capdevielle, Forschungszentrum Karlsruhe-Wissenschaftliche Berichte Report No. FZKA 6019, 1998 (unpublished).
- [16] G. Battistoni, F. Cerutti, A. Fassò, A. Ferrari, S. Muraro, J. Ranft, S. Roesler, and P. R. Sala, The FLUKA code: description and benchmarking, *AIP Conf. Proc.* **896**, 31 (2007).
- [17] A. Ferrari, P. Sala, A. Fassò, and J. Ranft, Report No. CERN-2005-10, INFN/TC_05/11, SLAC-R-773, 2005 (unpublished).
- [18] S. Ostapchenko, QGSJET-II: towards reliable description of very high energy hadronic interactions, *Nucl. Phys. B, Proc. Suppl.* **151**, 143 (2006).
- [19] T. Pierog and K. Werner, EPOS model and ultra high energy cosmic rays, *Nucl. Phys. B, Proc. Suppl.* **196**, 102 (2009).
- [20] S. Fletcher, T. Gaisser, P. Lipari, and T. Stanev, SIBYLL: An event generator for simulation of high energy cosmic ray cascades, *Phys. Rev. D* **50**, 5710 (1994).
- [21] S. Agostinelli *et al.* (GEANT4 Collaboration), Geant4—a simulation toolkit, *Nucl. Instrum. Methods Phys. Res., Sect. A* **506**, 250 (2003).
- [22] M. Aguilar *et al.*, Precision measurement of the proton flux in primary cosmic rays from rigidity 1 GV to 1.8 TV with the Alpha Magnetic Spectrometer on the International Space Station, *Phys. Rev. Lett.* **114**, 171103 (2015).
- [23] M. Aguilar *et al.*, Precision measurement of the helium flux in primary cosmic rays of rigidities 1.9 GV to 3 TV with the Alpha Magnetic Spectrometer on the International Space Station, *Phys. Rev. Lett.* **115**, 211101 (2015).
- [24] E. Thébault *et al.*, International Geomagnetic Reference Field: the 12th generation, *Earth Planets Space* **67**, 79 (2015).
- [25] J. E. Stone, D. Gohara, and G. Shi, OpenCL: A parallel programming standard for heterogeneous computing systems, *IEEE Design and Test of Computers* **12**, 66 (2010).
- [26] A. Klöckner, N. Pinto, Y. Lee, B. Catanzaro, P. Ivanov, and A. Fasih, PyCUDA and PyOpenCL: A scripting-based approach to GPU run-time code generation, *Parallel Comput.* **38**, 157 (2012).
- [27] J. P. Boris, *Proceedings of the Fourth Conference on Numerical Simulations of Plasmas* (Naval Research Laboratory, Washington D. C., 1970), p. 3.
- [28] C. Birdsall and A. Langdon, *Plasma Physics Via Computer Simulation* (McGraw-Hill, Inc., New York, 1985), p. 356.
- [29] K. Greisen, Cosmic ray showers, *Annu. Rev. Nucl. Sci.* **10**, 63 (1960).
- [30] N. Whitehorn, J. van Santen, and S. Lafebvre, Penalized splines for smooth representation of high-dimensional Monte Carlo datasets, *Comput. Phys. Commun.* **184**, 2214 (2013).
- [31] A. U. Abeysekara *et al.*, Observation of small-scale anisotropy in the arrival direction distribution of TeV cosmic rays with HAWC, *Astrophys. J.* **796**, 108 (2014).
- [32] R. W. Atkins *et al.*, Observation of TeV gamma rays from the Crab Nebula with Milagro using a new background rejection technique, *Astrophys. J.* **595**, 803 (2003).
- [33] A. Abeysekara *et al.* (HAWC Collaboration), in *Proceedings of 33rd International Cosmic Ray Conference, Rio de Janeiro, 2013* [[arXiv:1310.0071](https://arxiv.org/abs/1310.0071)].
- [34] G. D'Agostini, A multidimensional unfolding method based on Bayes' theorem, *Nucl. Instrum. Methods Phys. Res., Sect. A* **362**, 487 (1995).
- [35] A. N. Kolmogorov, Sulla determinazione empirica di una legge di distribuzione, *G. Ist. Ital. Attuari* **4**, 83 (1933).
- [36] N. Smirnov, Table for estimating the goodness of fit of empirical distributions, *Ann. Math. Stat.* **19**, 279 (1948).
- [37] Z. Hampel-Arias, Ph.D. thesis, University of Wisconsin—Madison, 2017.
- [38] T. K. Gaisser, Spectrum of cosmic-ray nucleons, kaon production, and the atmospheric muon charge ratio, *Astropart. Phys.* **35**, 801 (2012).
- [39] J. Hörandel, On the knee in the energy spectrum of cosmic rays, *Astropart. Phys.* **19**, 193 (2003).
- [40] T. K. Gaisser, T. Stanev, and S. Tilav, Cosmic ray energy spectrum from measurements of air showers, *Front. Phys.* **8**, 748 (2013).
- [41] M. G. Aartsen *et al.*, Measurement of the cosmic ray energy spectrum with IceTop-73, *Phys. Rev. D* **88**, 042004 (2013).
- [42] B. Bartoli *et al.*, Light-component spectrum of the primary cosmic rays in the multi-TeV region measured by the ARGO-YBJ experiment, *Phys. Rev. D* **85**, 092005 (2012).